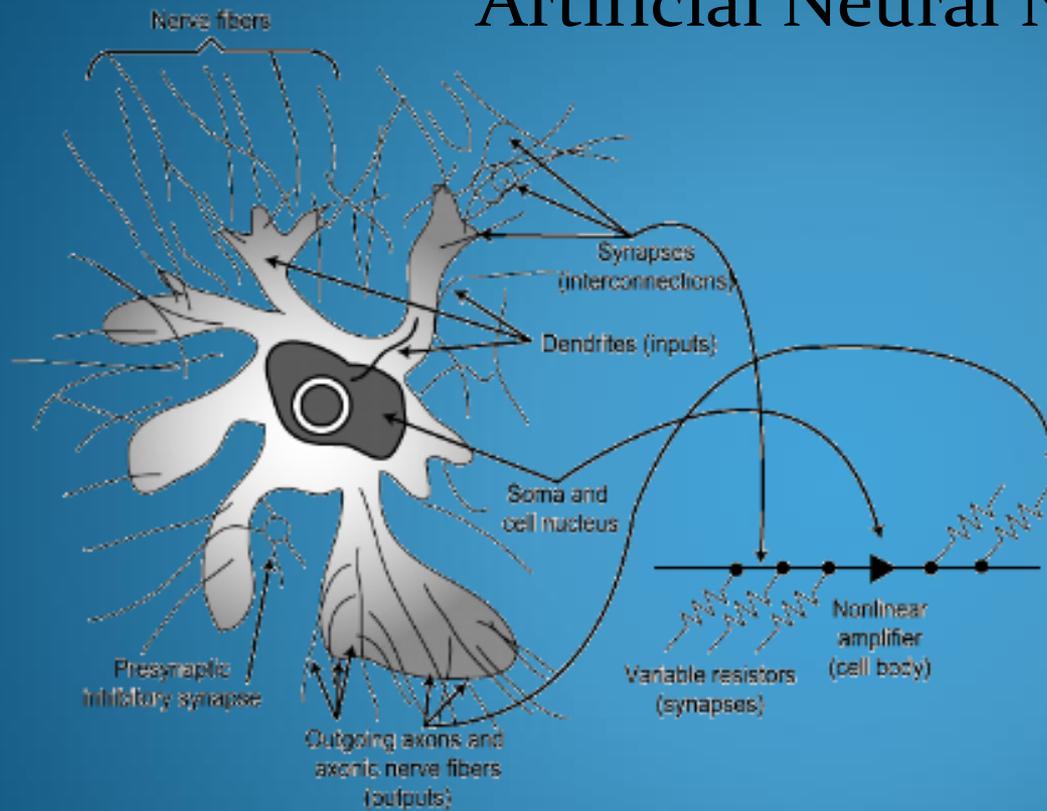


# Artificial Neural Networks





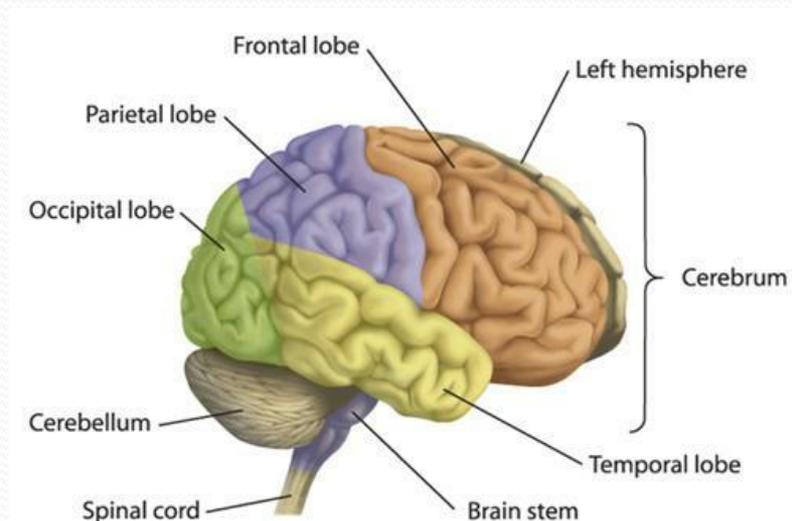
# BIOLOGICAL INSPIRATION OF NN

# Neural Networks

- Analogy to biological neural systems,
- Attempt to understand natural biological systems through computational modeling.
- Massive parallelism allows for computational efficiency.
- Intelligent behavior as an “emergent” property of large number of simple units rather than from explicitly encoded symbolic rules and algorithms.

# Biological Inspiration

- The brain has been extensively studied by scientists.
- Vast complexity prevents all but rudimentary understanding.
- Even the behaviour of an individual neuron is extremely complex
- Engineers **modified the neural models to make them** more useful
  - less like biology
  - kept much of the terminology



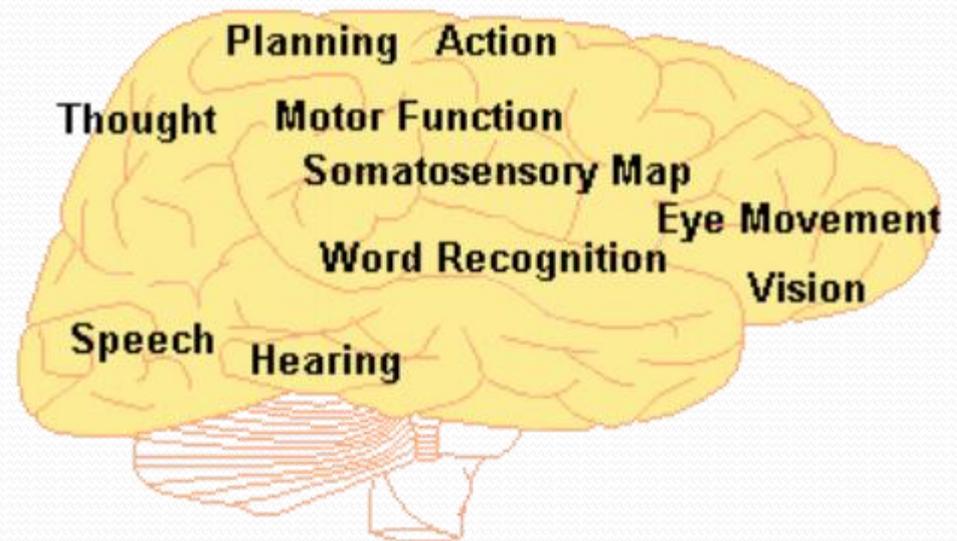
# The Biological Neural Network

## Characteristics of Human Brain

- Ability to learn from experience
- Ability to generalize the knowledge it possess
- Ability to perform abstraction
- To make errors

## Objective

- To emulate or simulate the human brain.

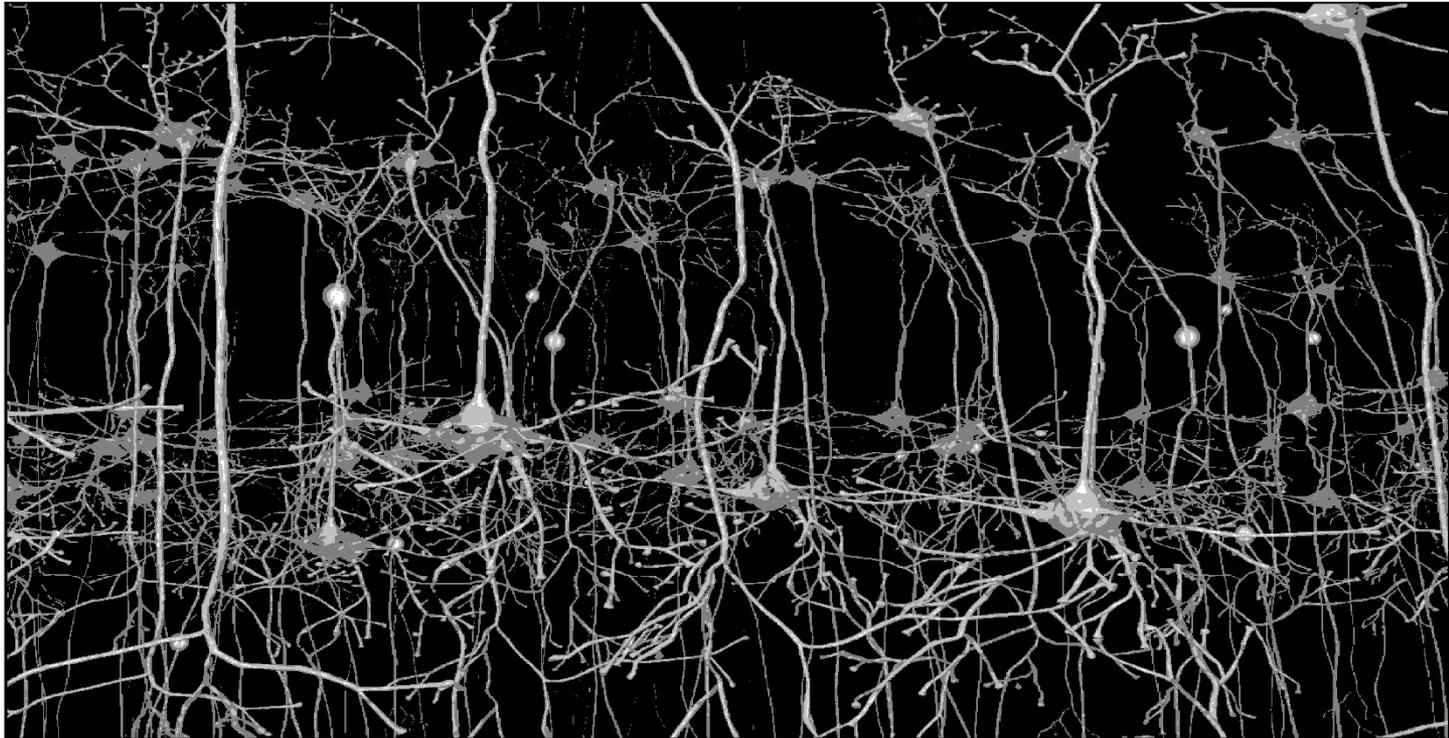


# Organization of Human Brain

Stimulus → Receptors ↔ Neural net ↔ Effectors → Response

- Over one hundred billion neurons.
- Over one hundred trillion connections called synapses.
- Neurons are responsible for thought emotion, cognition etc.
- Consists of a dense network blood vessels.

# Real Neurons



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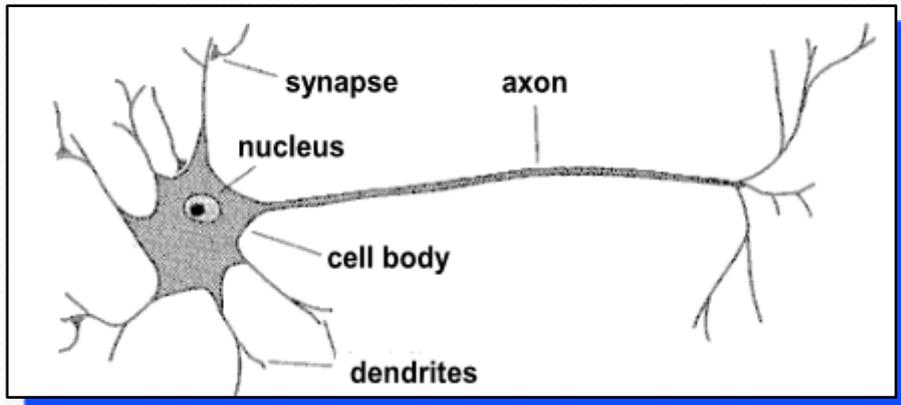
DIGITAL STUDIO SA

CG image of the vertical organization of neurons in the primary visual cortex (V1).  
*Smooth stellate and spiny stellate cells relay visual information coming out from the retina to pyramidal cells, themselves doing a first basic computation of visual motion perception.*  
version of July 2000

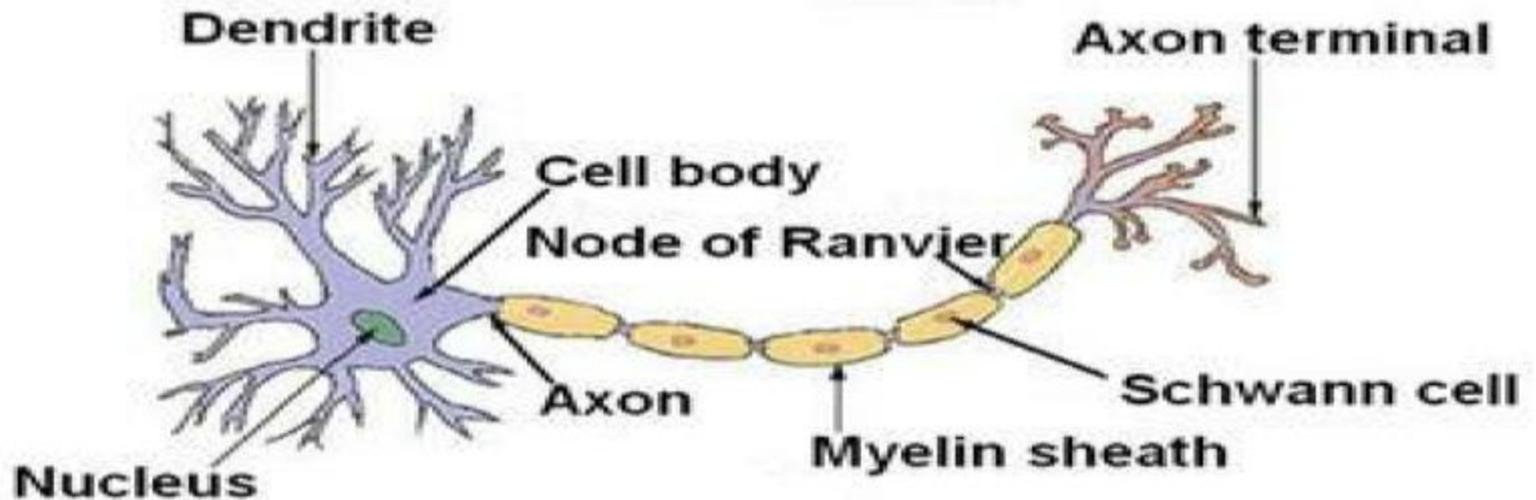
- The brain is a collection of about 10 billion interconnected neurons
- Each neuron is a cell that uses biochemical reactions to receive, process and transmit information

# The Neuron

- Fundamental building block of the nervous system
- Performs all the computational and communication functions within the brain
- A many inputs/ one output unit



# Structure of a Typical Neuron



The biological neuron has four main regions to its structure

1. The cell body, or soma
2. The axon
3. The dendrites
4. Synapse

# Cell body

- It is the heart of the cell. It contains the nucleolus and maintains protein synthesis
- manufactures a wide variety of complex molecules, to keep it renewed for a life time
- manages the energy economy of the neuron
- the outer membrane of the cell body generates nerve impulses.
- Cell body is 5 to 100 microns in dia

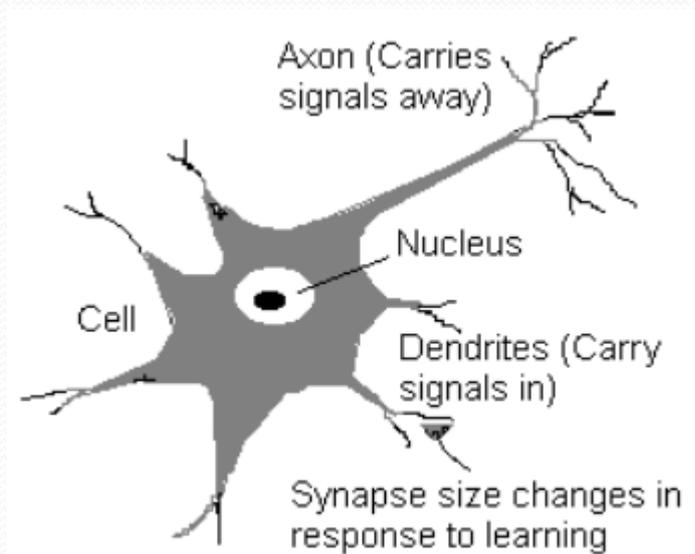
# The Axon

- May be as short as 0.1 mm or it is 1 m in length.
- Has multiple branches each terminating in a *synapse*.
- The axon main purpose is to conduct electrical signals generated at the axon down its length. These signals are called *action potentials*

- The other end of the axon may split into several branches, which end in a **pre-synaptic** terminal.
- The myelin is a fatty issue that insulates the axon. The non-insulated parts of the axon area are called **Nodes of Ranvier**.
- At these nodes, the signal traveling down the axon is regenerated. This ensures that the signal travel down the axon to be fast and constant.
- The brain analyzes all patterns of signals sent, and from that information it interprets the type of information received

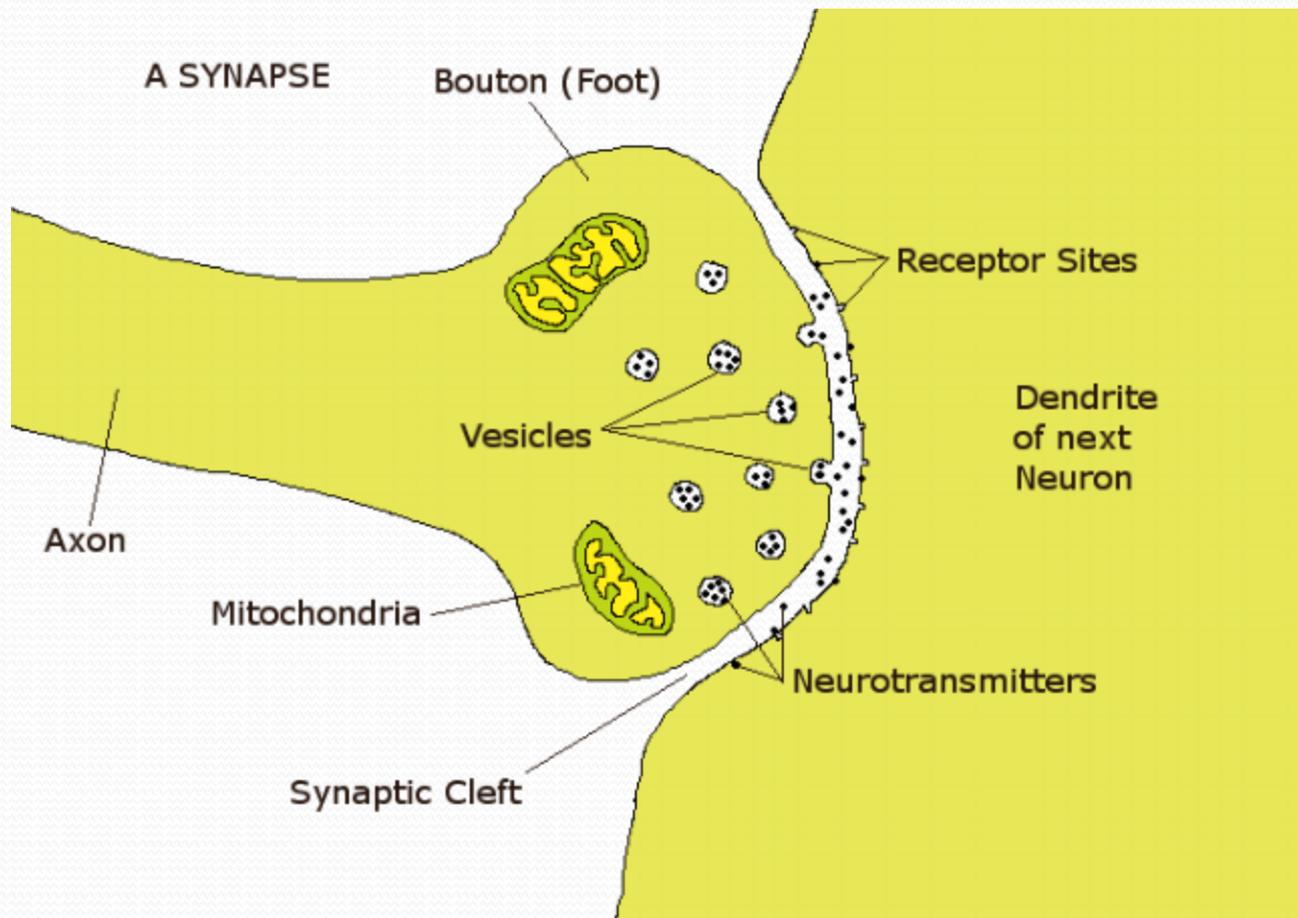
# Dendrites

- bushy branching structure emanating from the cell body.
- Receive the signals from other cells at connection points called **synapses**.
- Usually no physical or electrical connection made at the synapse
- A neuron's dendritic tree is connected to a thousand neighbouring neurons (10,000)



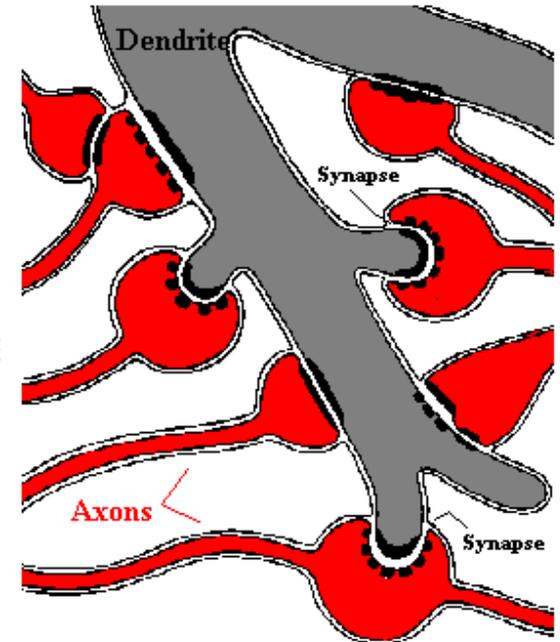
# Synapse

- The synapse is the area of contact between two neurons.
- They do not physically touch because they are separated by a cleft.
- The electric signals are sent through chemical interaction.
- The neuron sending the signal is called *pre-synaptic cell* and the neuron receiving the electrical signal is called *postsynaptic cell*.



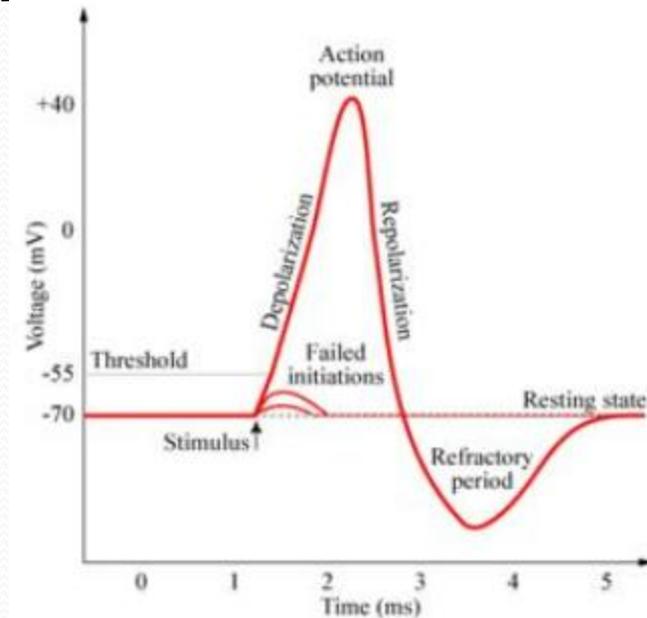
# The Bio Neuron

- Neurotransmitters which are specialized chemicals are released by the axon, into the synaptic cleft, diffuse across to the dendrite.
  - When one of those neurons fire, a positive or negative charge is received by one of the dendrites. The strengths of all the received charges are added together through the processes of spatial and temporal summation.
- A neuron only fires if its input signal exceeds a certain amount (**threshold**) in a short time period.
  - Neurotransmitters are **excitatory**, which tend to produce a output pulse.
  - Some are **inhibitory**, which tend to suppress such a pulse



# Neural Communication

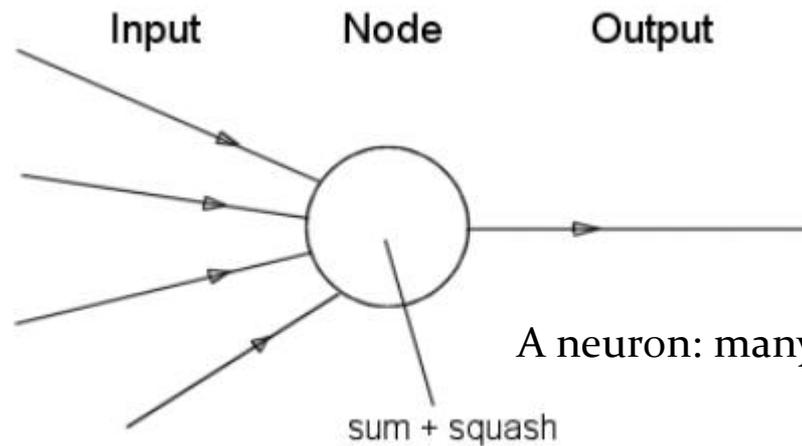
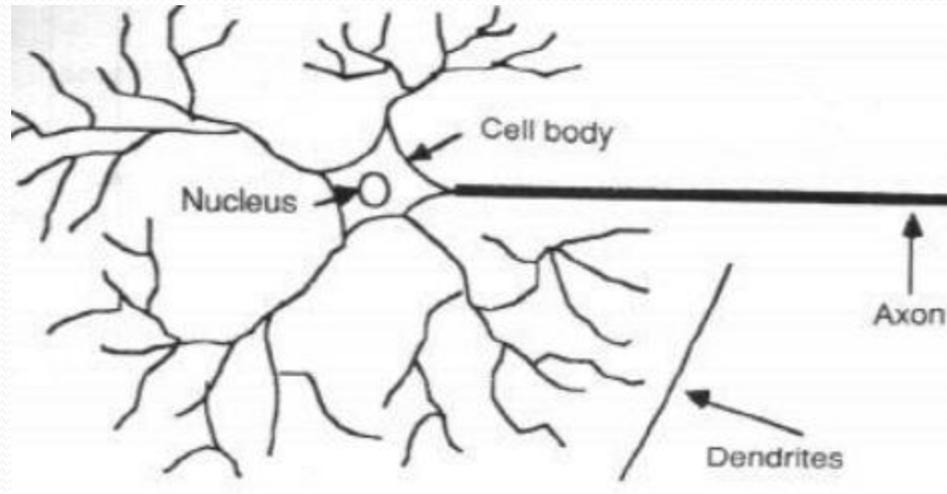
- Electrical potential across cell membrane exhibits spikes called action potentials.
- Spike originates in cell body, travels down axon, and causes synaptic terminals to release neurotransmitters.
- Chemical diffuses across synapse to dendrites of other neurons.
- If net input of neurotransmitters to a neuron from other neurons is excitatory and exceeds some threshold, it fires an action potential.





# **BIO NEURON NETWORK TO ARTIFICIAL NEURON NETWORK**

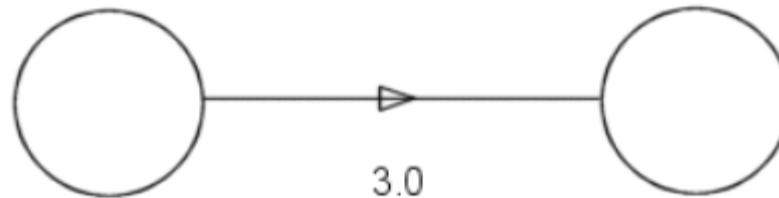
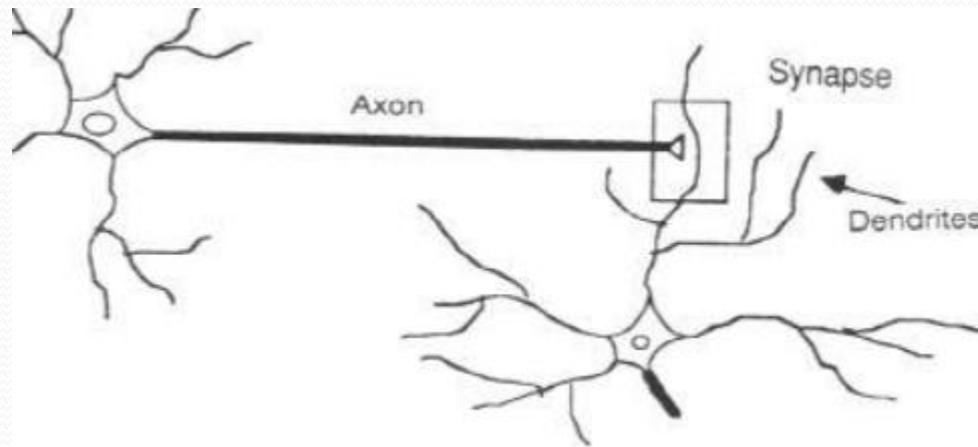
# Neuron vs. Node

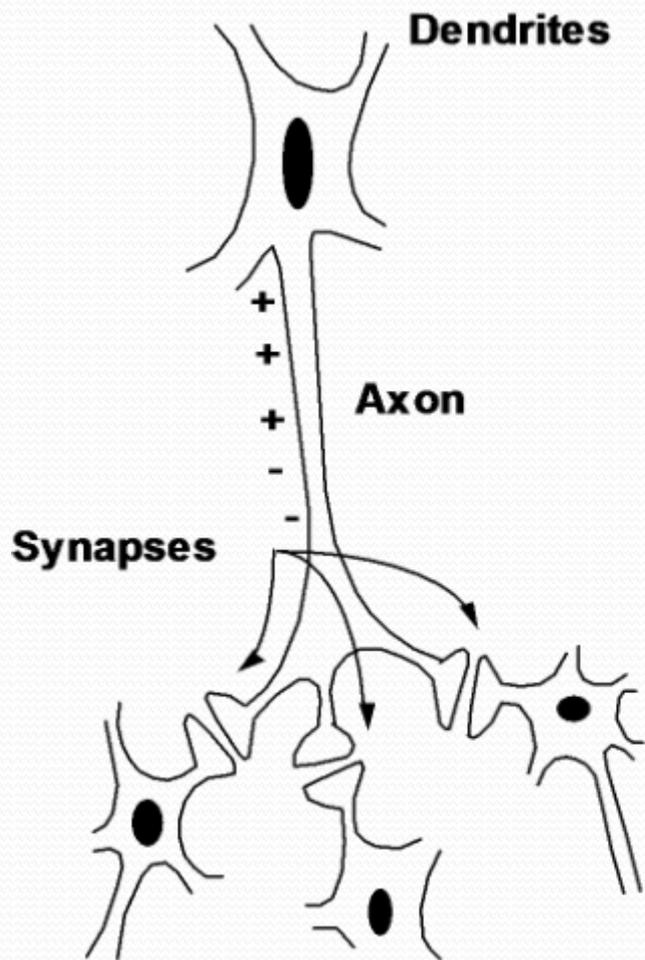


A neuron: many-inputs / one-output unit

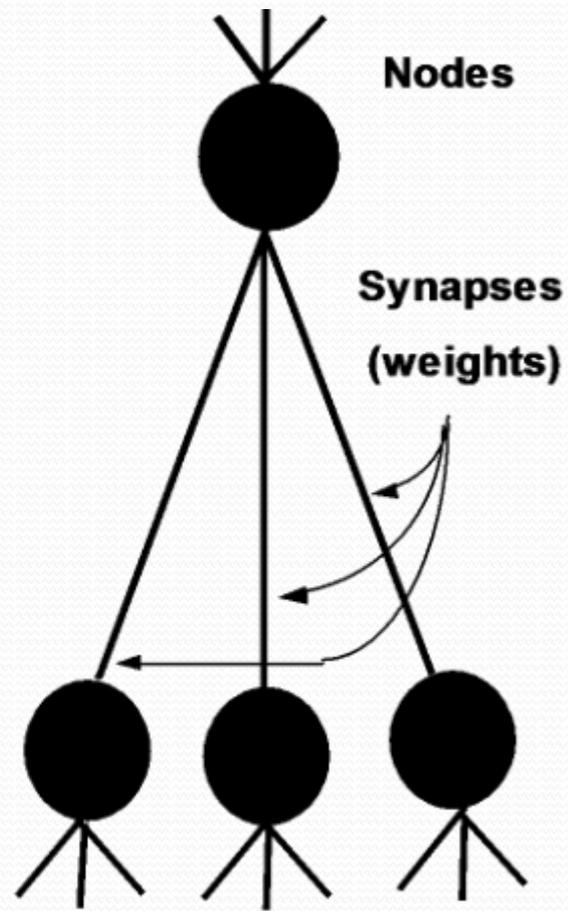
# Synapse vs weight

--Axon turn the processed inputs to outputs. --- Synapses are the electrochemical contact between neurons.





Impulse



- Each neuron **receives inputs from** other neurons
  - *A few neurons also connect to receptors.*
  - *Cortical neurons use spikes to communicate.*
- The effect of each input line on the neuron is **controlled by a synaptic weight**
  - *The weights can be positive or negative.*
- The synaptic weights **adapt** so that the whole network learns to **perform useful computations**
  - *Recognizing objects, understanding language, making plans, controlling the body.*
- We have about  **$10^{11}$**  neurons each with about  **$10^4$**  weights.
  - *A huge number of weights can **affect the computation** in a very short time.*

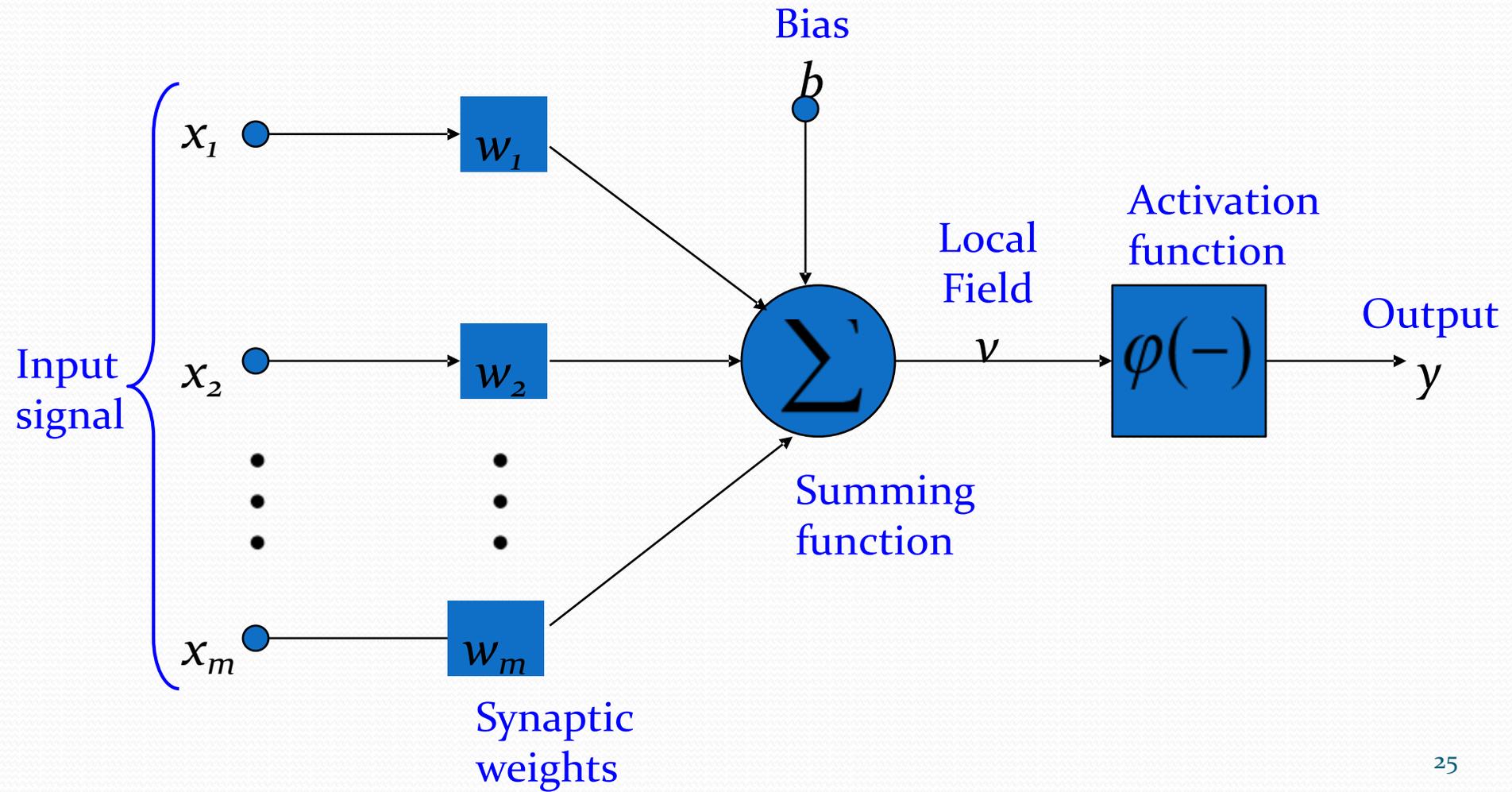
# Idealized neurons

- To model things we have to idealize them
  - Idealization removes complicated details that are not essential for understanding the main principles.
  - It allows us to apply mathematics and to make analogies to other, familiar systems.
  - Once we understand the basic principles, its easy to add complexity to make the model more faithful.

# Artificial neural networks

- An artificial neural network is composed of many artificial neurons that are linked together according to a specific network architecture.
- Signals (action potentials) appear at the node's inputs (synapses).
- The each input is multiplied by a certain weight, before being added together at the node (neuron) to produce an overall activation.
- If this exceeds a threshold, the node fires, sending signals to other nodes.

# The Artificial Neuron



# The Neuron

- The neuron is the basic information processing unit of a NN.
- It consists of:
  - 1 A set of **synapses** or **connecting links**, each link characterized by a **weight**:  $(W_{kj})$   
 $W_1, W_2, \dots, W_m$
  - 2 An **adder** function (**combiner**) which computes the weighted sum of the inputs:  
$$u = \sum_{j=1}^m w_j x_j$$

3 **Activation function** (squashing function) for limiting the amplitude of the output of the neuron

$Y = \text{activation potential} / \text{induced local field}$

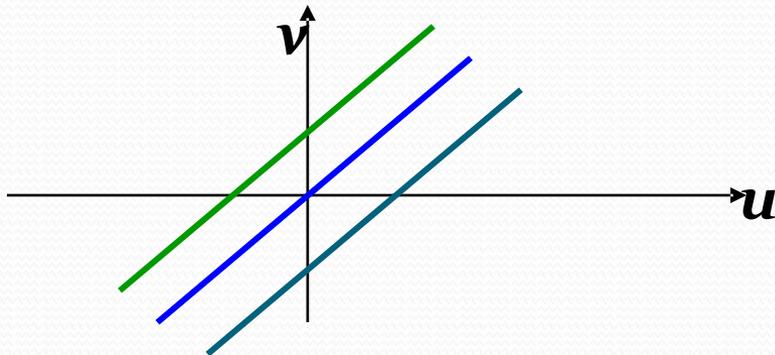
$$y = \varphi(u + b)$$

# Bias of a Neuron

- Bias  $b$  has the effect of applying an affine transformation to  $u$

$$v = u + b$$

- $v$  is the **induced field** of the neuron



# Linear neurons

- These are simple but computationally limited
  - If we can make them learn we **may** get insight into more complicated neurons.

$$y = b + \sum_i x_i w_i$$

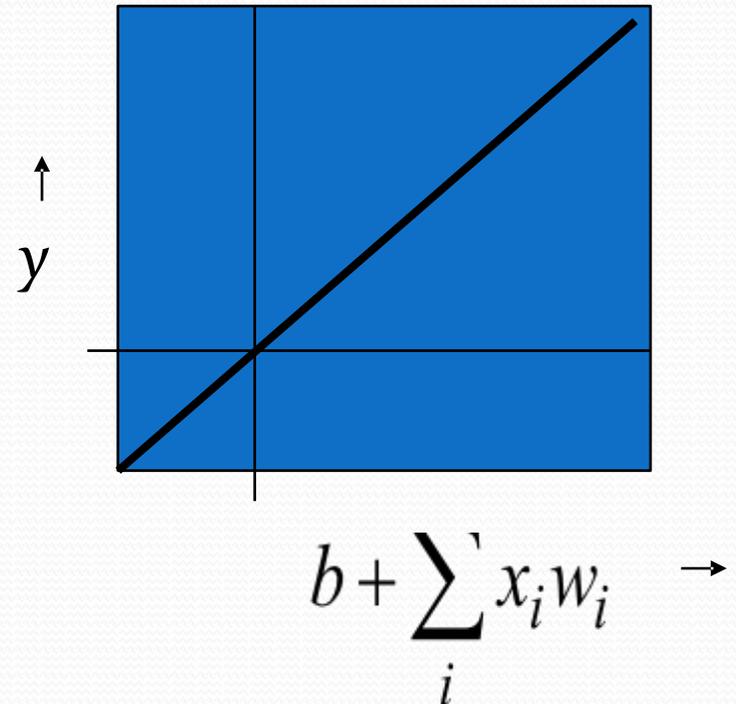
output ↑

↑ bias

↑  $i^{\text{th}}$  input

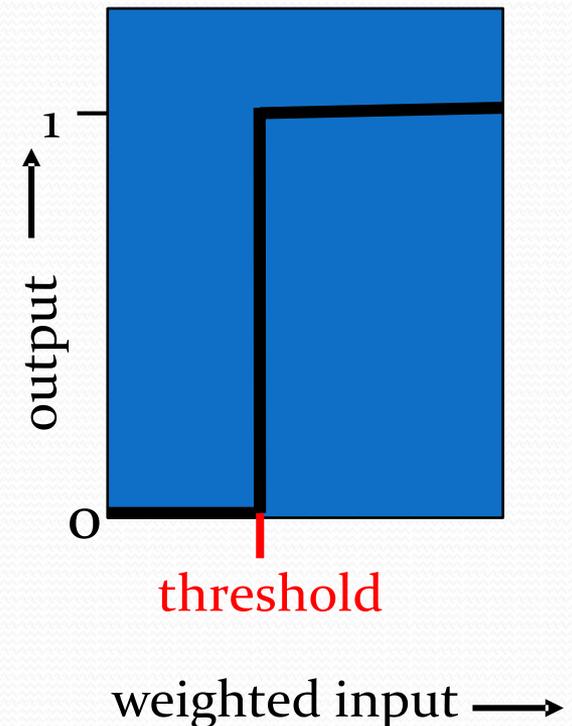
↑  $i$  index over input connections

weight on  $i^{\text{th}}$  input



# Binary threshold neurons

- McCulloch-Pitts (1943): **influenced Von Neumann.**
  - First compute a weighted sum of the inputs.
  - Then send out a fixed size spike of activity if the weighted sum exceeds a threshold.
  - McCulloch and Pitts thought that each spike is like the truth value of a proposition and each neuron combines truth values to compute the truth value of another proposition!



# Binary threshold neurons

- There are two equivalent ways to write the equations for a binary threshold neuron:

$$u = \sum_i x_i w_i$$

$$v = b + \sum_i x_i w_i$$

$$\theta = -b$$

$$\varphi(v) = \begin{cases} 1 & \text{if } v \geq \theta \\ 0 & \text{otherwise} \end{cases}$$

$$y = \begin{cases} 1 & \text{if } v \geq 0 \\ 0 & \text{otherwise} \end{cases}$$

# Rectified Linear Neurons

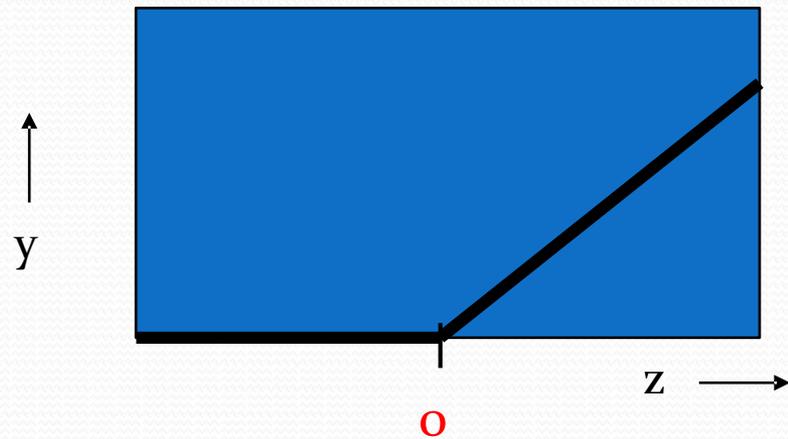
(sometimes called linear threshold neurons)

They compute a **linear** weighted sum of their inputs.

The output is a **non-linear** function of the total input.

$$v = b + \sum_i x_i w_i$$

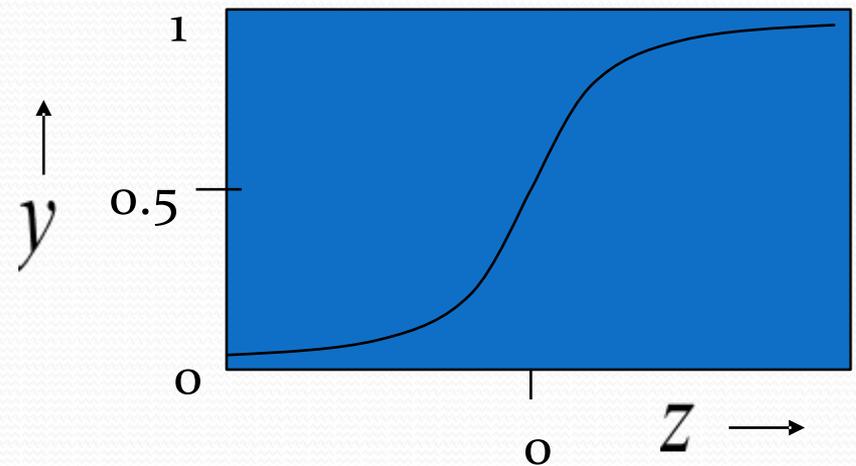
$$y = \begin{cases} v & \text{if } v > 0 \\ 0 & \text{otherwise} \end{cases}$$



# Sigmoid neurons

- These give a real-valued output that is a smooth and bounded function of their total input.
  - Typically they use the logistic function
  
- They have nice derivatives which make learning easy

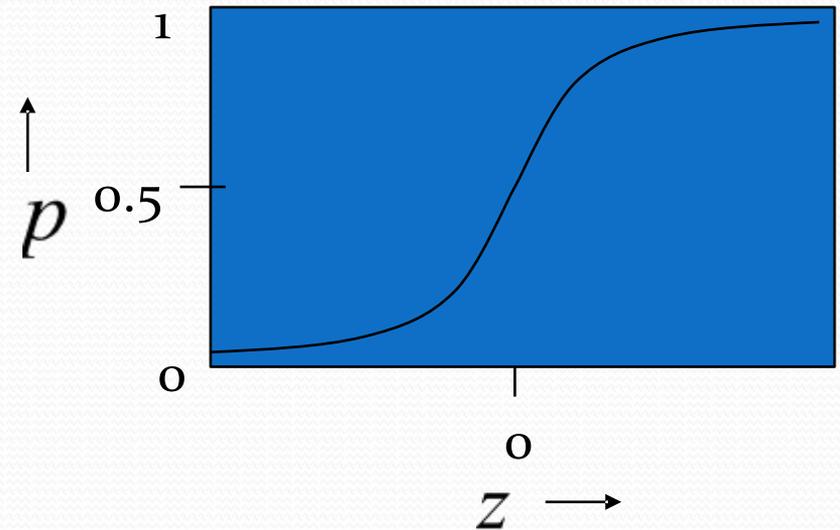
$$v = b + \sum_i x_i w_i \quad y = \frac{1}{1 + e^{-av}}$$



# Stochastic binary neurons

- These use the same equations as logistic units.
  - But they treat the output of the logistic as the **probability** of producing a spike in a short time window.
- We can do a similar trick for rectified linear units:
  - The output is treated as the Poisson rate for spikes.

$$z = b + \sum_i x_i w_i \quad p(s=1) = \frac{1}{1 + e^{-z}}$$



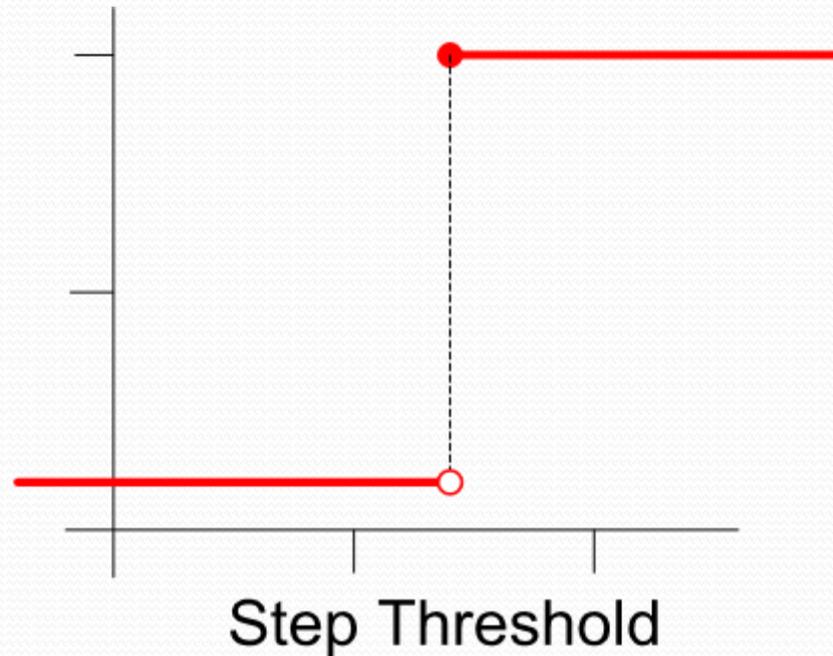
# ACTIVATION FUNCTIONS

- To calculate the output response of a neuron
- Transforms neuron's input into output.
- Features of activation functions:
  - A squashing effect is required
    - Prevents accelerating growth of activation levels through the network.
  - Simple and easy to calculate

# Threshold Activation Function

- Binary classifier functions

Heaveside function



# Binary Threshold Signal Function

- The threshold logic neuron is a two state machine

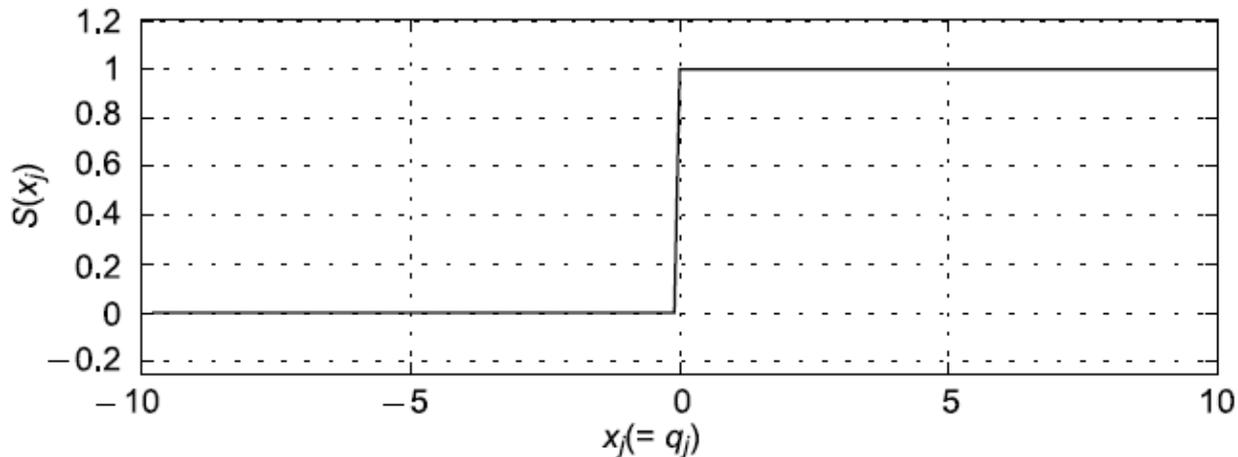
- $s = S(x) \in \{0, 1\}$

- Net positive activations translate to a +1 signal value
- Net negative activations translate to a 0 signal value.

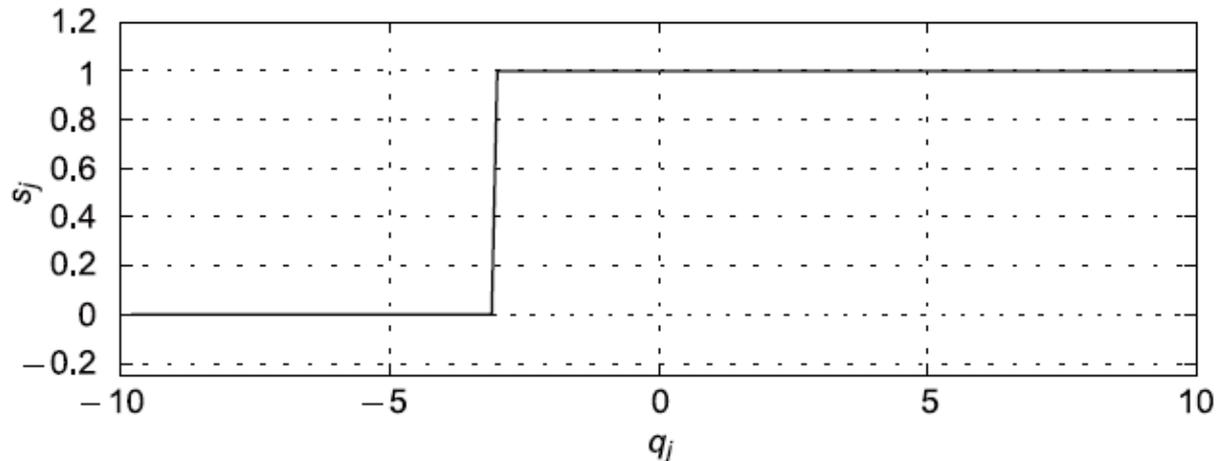
$$\Phi(v) = \begin{cases} 1 & v \geq 0 \\ 0 & v < 0 \end{cases}$$

$$Y_k = \begin{cases} 1 & v \geq 0 \\ 0 & v < 0 \end{cases}$$

# Neuron Signal Functions: Binary Threshold Signal Function



(a) Binary threshold function:  $\theta_j = 0$

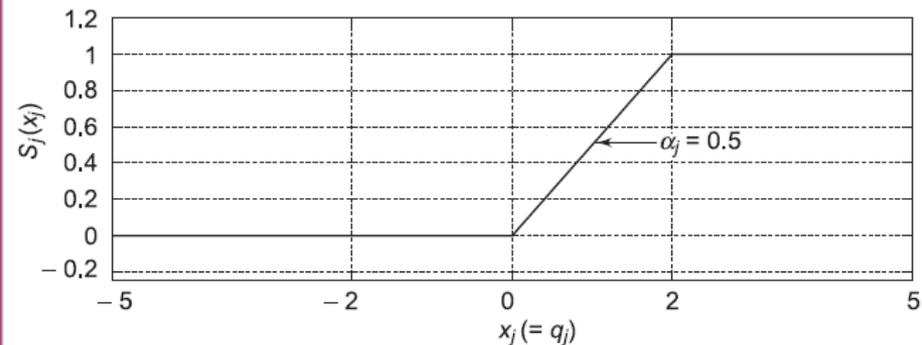


(b) Binary threshold function:  $\theta_j = +3$

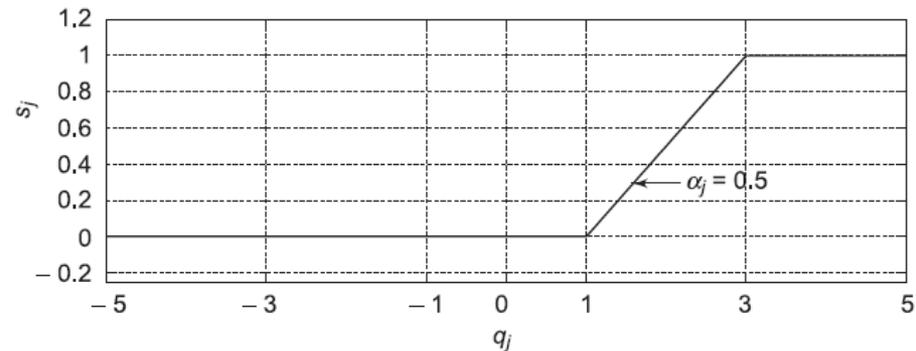
# Linear Threshold Signal Function

$$S_j(x_j) = \begin{cases} 0 & x_j \leq 0 \\ \alpha_j x_j & 0 < x_j < x_m \\ 1 & x_j \geq x_m \end{cases}$$

- $\alpha_j = 1/x_m$  is the **slope parameter** of the function
- Figure plotted for  $x_m = 2$  and  $\alpha_j = 0.5$ .



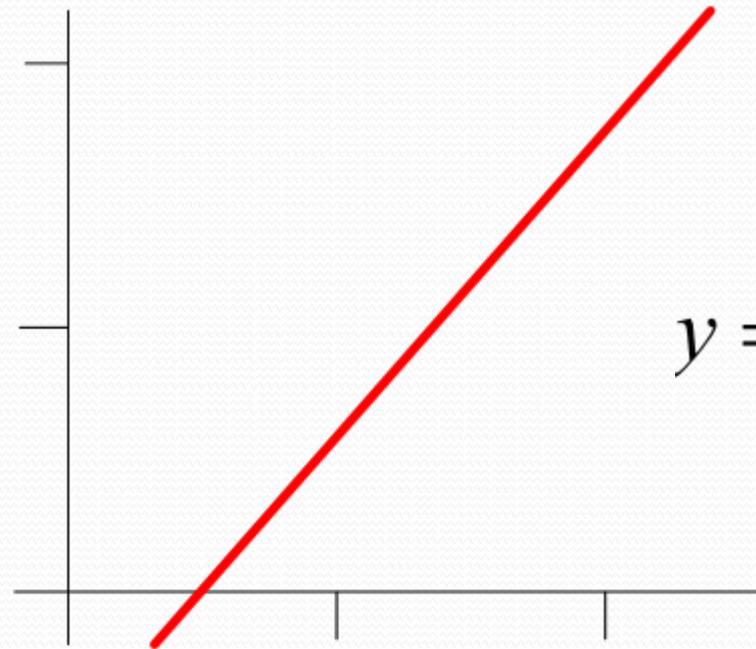
(a) Linear Threshold function:  $\theta_j = 0$



(b) Shifted Linear Threshold function:  $\theta_j = -1$

# Linear Activation functions

- Output is scaled sum of inputs



$$y = u = \sum_{n=1}^N w_n x_n$$

Linear

# Threshold Logic Neuron (TLN) in Discrete Time

- The updated signal value  $S(x_j^{k+1})$  at time instant  $k + 1$  is generated from the neuron activation  $x_j^{k+1}$ , sampled at time instant  $k + 1$ .
- The response of the threshold logic neuron as a two-state machine can be extended to the *bipolar* case where the signals are
  - $s \in \{-1, 1\}$

$$S(x_j^{k+1}) = \begin{cases} 1 & x_j^{k+1} > 0 \\ S(x_j^k) & x_j^{k+1} = 0 \\ 0 & x_j^{k+1} < 0 \end{cases}$$

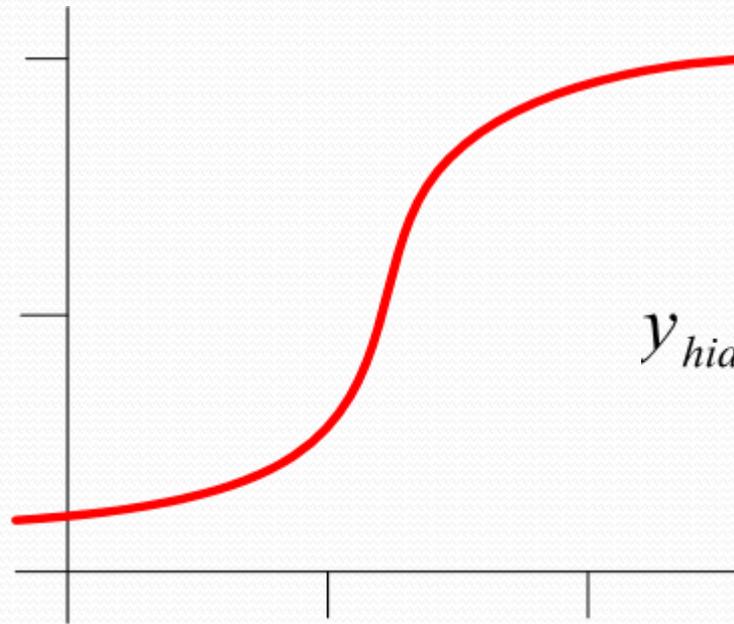
$$S(x_j) = \begin{cases} +1 & x_j > 0 \\ -1 & x_j < 0 \end{cases}$$

# Threshold Logic Neuron (TLN) in Discrete Time

- The resulting signal function is then none other than the *signum function*,  $\text{sign}(x)$  commonly encountered in communication theory.

# Nonlinear Activation Functions

- Sigmoid Neuron unit function



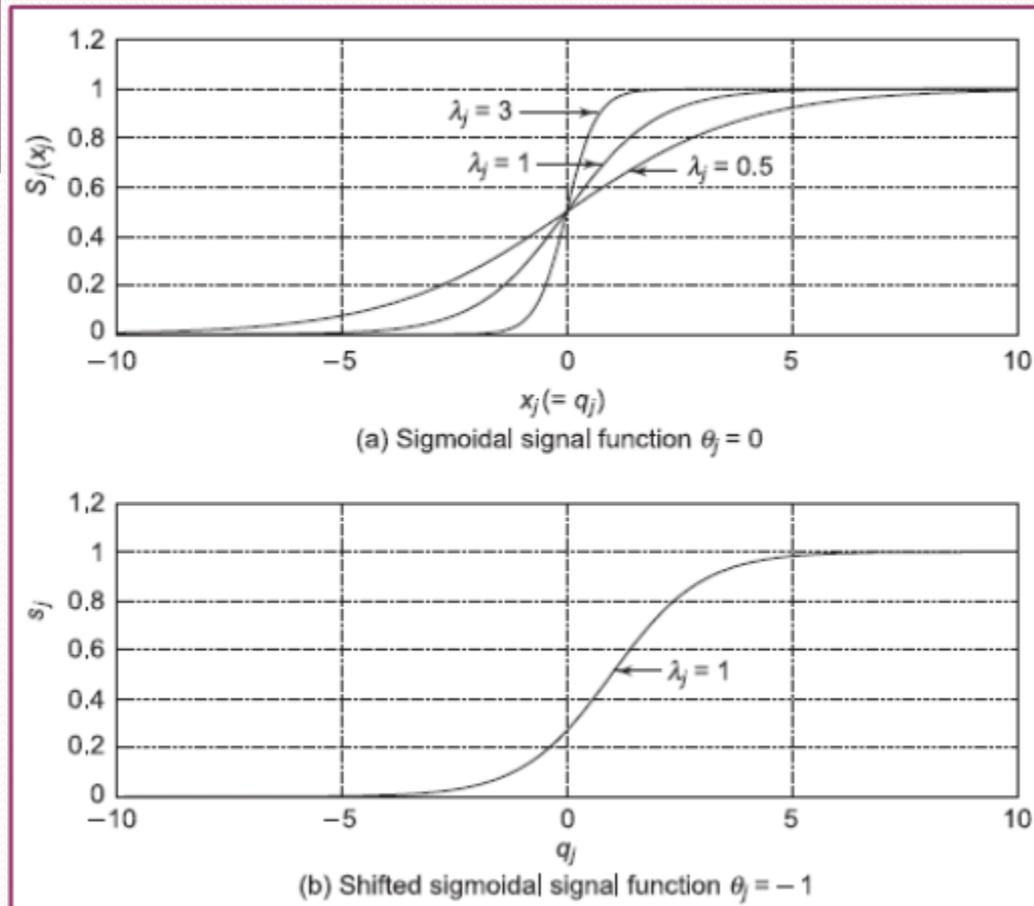
$$y_{hid}(u) = \frac{1}{1 + e^{-u}}$$

Sigmoid

# Sigmoidal Signal Function

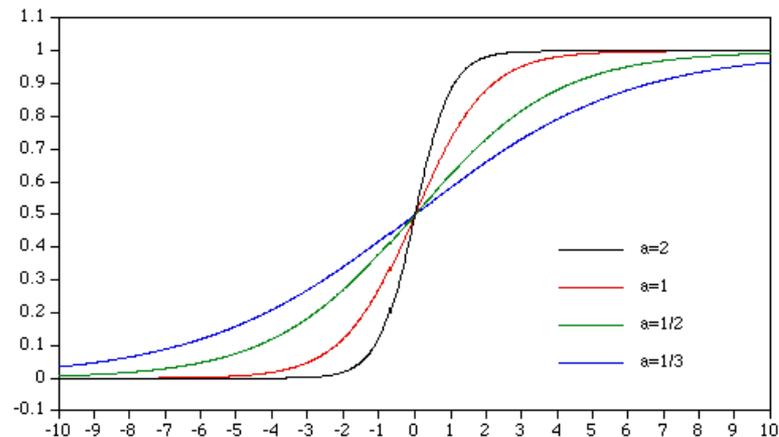
$$S_j(x_j) = \frac{1}{1 + e^{-\lambda_j x_j}}$$

- $\lambda_j$  is a gain scale factor
- In the limit, as  $\lambda_j \rightarrow \infty$  the smooth logistic function approaches the non-smooth binary threshold function.



# Activation Function

- Squashing Function or Logistic Function or Sigmoid Function.



$$Y = \frac{1}{1 + e^{-f}}$$

$$f = 0$$

$$Y = 0.5$$

$$f > 0$$

$$Y = 1$$

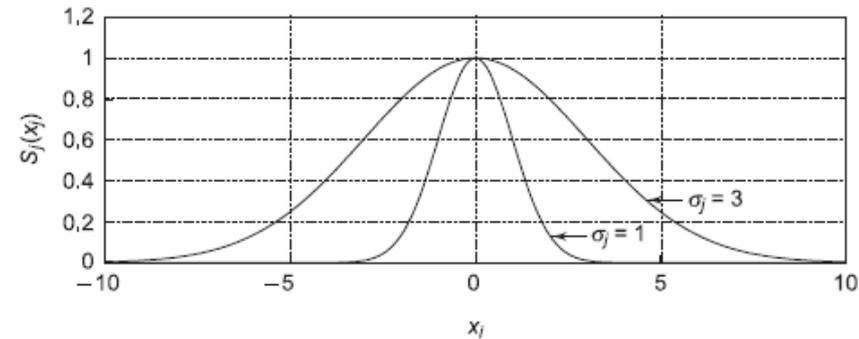
$$f < 0$$

$$Y = 0$$

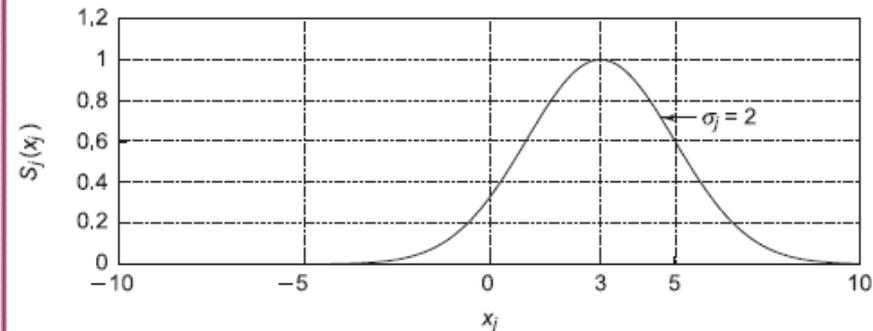
# Gaussian Signal Function

$$S_j(x_j) = \exp\left(-\frac{(x_j - c_j)^2}{2\sigma_j^2}\right)$$

- $\sigma$  is the Gaussian spread factor and  $c_j$  is the center.
- Varying the spread makes the function sharper or more diffuse.



(a) Gaussian signal function: center = 0



(b) Gaussian signal function: center = 3

# Stochastic Neurons

- The signal is assumed to be two state
  - $s \in \{0, 1\}$  or  $\{-1, 1\}$
- Neuron switches into these states depending upon a *probabilistic function of its activation*,  $P(x_j)$ .

$$P(x_j) = \frac{1}{1 + e^{-x_j/T}}$$

# Summary of Signal Functions

| <i>Name</i>        | <i>Function</i>   | <i>Characteristics</i>   |
|--------------------|---|--|
| Binary threshold   | $\mathcal{S}(x_j) = \begin{cases} 1 & x_j \geq 0 \\ 0 & x_j < 0 \end{cases}$  | Non-differentiable, step-like, $s_j \in \{0, 1\}$              |
| Bipolar threshold  | $\mathcal{S}(x_j) = \begin{cases} 1 & x_j \geq 0 \\ -1 & x_j < 0 \end{cases}$   | Non-differentiable, step-like, $s_j \in \{-1, 1\}$             |
| Linear             | $\mathcal{S}_j(x_j) = \alpha_j x_j$   | Differentiable, unbounded, $s_j \in (-\infty, \infty)$         |
| Linear threshold   | $\mathcal{S}_j(x_j) = \begin{cases} 0 & x_j \leq 0 \\ \alpha_j x_j & 0 < x_j < x_m \\ 1 & x_j \geq x_m \end{cases}$               | Differentiable, piece-wise linear, $s_j \in [0, 1]$            |
| Sigmoid            | $\mathcal{S}_j(x_j) = \frac{1}{1 + e^{-\lambda_j x_j}}$   | Differentiable, monotonic, smooth, $s_j \in (0, 1)$            |
| Hyperbolic tangent | $\mathcal{S}_j(x_j) = \tanh(\lambda_j x_j)$   | Differentiable, monotonic, smooth, $s_j \in (-1, 1)$           |
| Gaussian           | $e^{-(x_j - c_j)^2 / 2\sigma_j^2}$  | Differentiable, non-monotonic, smooth, $s_j \in (0, 1)$        |
| Stochastic         | $\mathcal{S}_j(x_j) = \begin{cases} +1 & \text{with probability } P(x_j) \\ -1 & \text{with probability } 1 - P(x_j) \end{cases}$ | Non-deterministic step-like, $s_j \in \{0, 1\}$ or $\{-1, 1\}$ |



THANK YOU